

# Mod 8.5.17 [4]

Die  $n-1$   $x$ -Variablen, die Wert 1 haben,  
sind per Konstruktion

$$x_{j^{(1)}, j^{(2)}} , x_{j^{(2)}, j^{(3)}} , \dots , x_{j^{(n-1)}, j^{(n)}} \quad (5)$$

Wegen (3) gilt also insbesondere

$$\underbrace{p_{j^{(1)}}}_1 < p_{j^{(2)}} < p_{j^{(3)}} < \dots < p_{j^{(n-1)}} < \underbrace{p_{j^{(n)}}}_n$$

Wegen  $p_i \in [n] \forall i \in [n]$  ist also

$$p_1 = 1, p_{j^{(2)}} = 2, p_{j^{(3)}} = 3, \dots, p_{j^{(n-1)}} = n-1, p_n = n,$$

d.h.  $i \mapsto p_i$  ist die Umkehr-Bijektion  
zu  $j \mapsto j^{(j)}$  mit (wegen (5))

$$x_{ij} = 1 \Leftrightarrow p_j = p_{i+1}$$

□

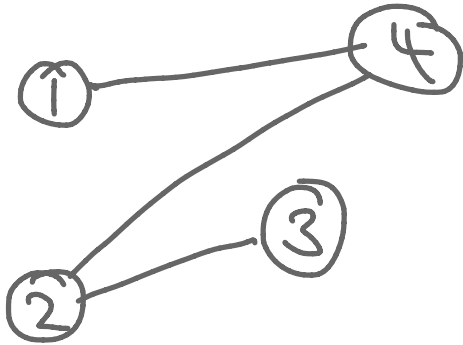
↑  
[a]

[10]

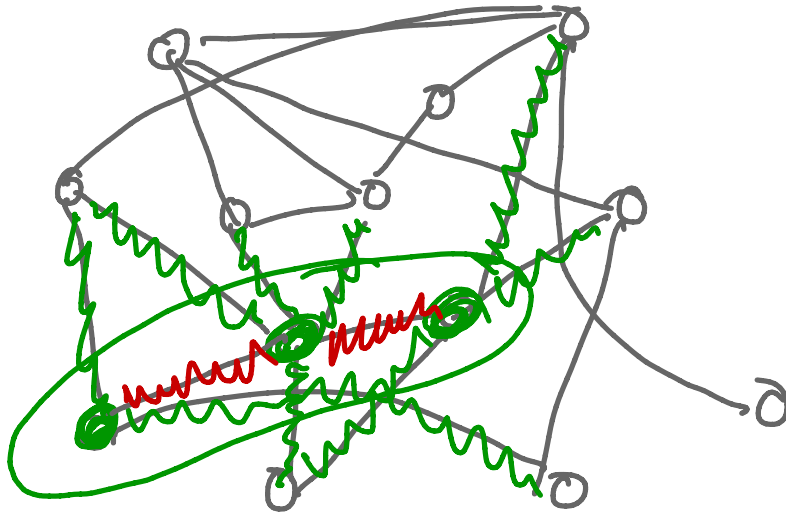
$$G = (V, E)$$

$$V = \{1, 2, 3, 4\}$$

$$E = \{\{1, 4\}, \{2, 3\}, \{2, 4\}\}$$

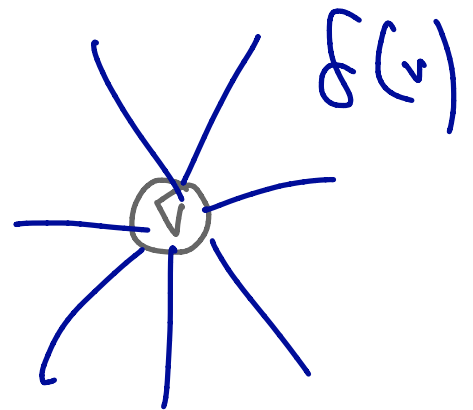
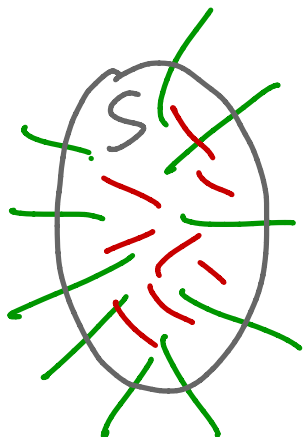


[11]



$\delta(S)$

$E(S)$



[12]  $G$  is graph

$$\left| \{(v, e) : v \in V(G), e \in E(G), v \in e\} \right|$$

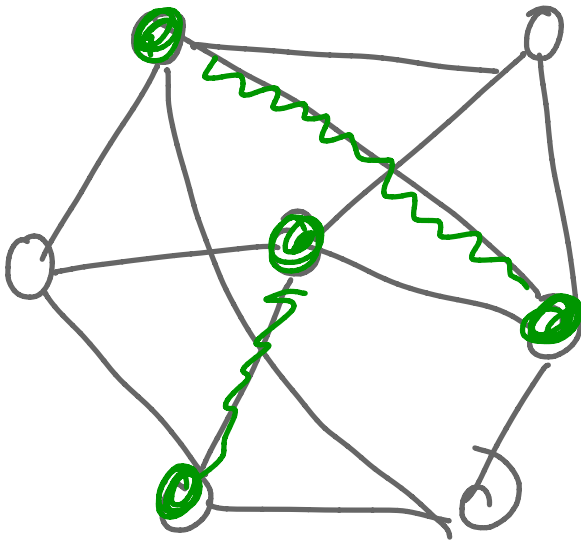
$$\sum_{e \in E(G)} \underbrace{\left| \{v \in V(G) : v \in e\} \right|}_2$$

$$\parallel \\ 2 \cdot |E(G)|$$

$$\sum_{v \in V(G)} \underbrace{\left| \{e \in E(G) : v \in e\} \right|}_{d(v)}$$

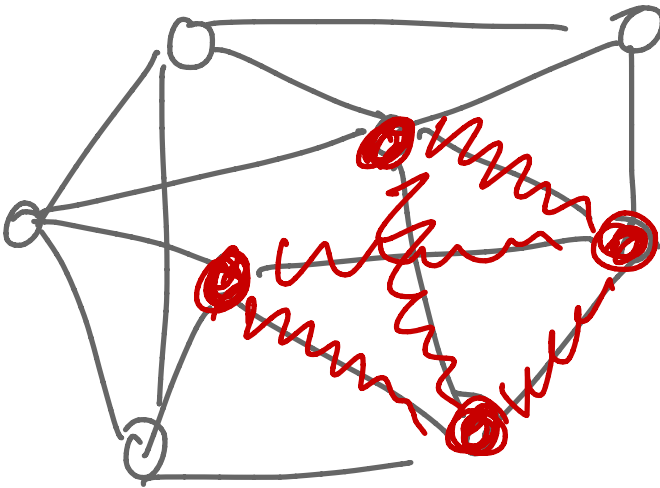
$$\Rightarrow \sum_{v \in V(G)} d(v) \in 2\mathbb{Z}$$

[13]



Untergaph,  
nicht spanned,  
nicht induziert

[14]



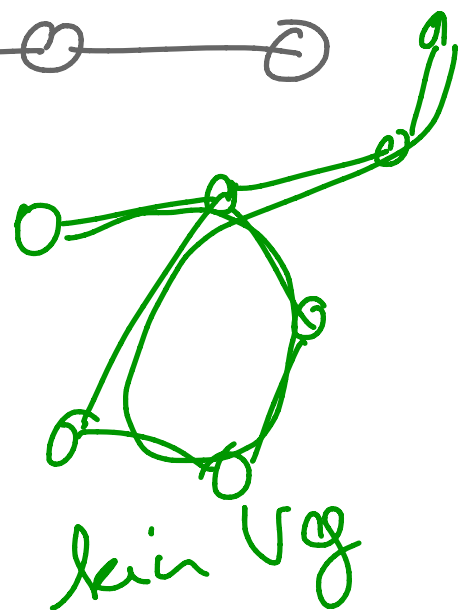
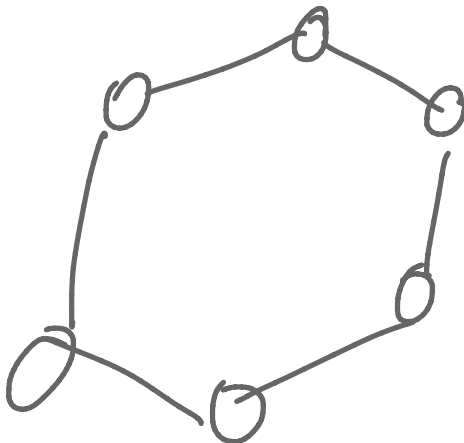
induzierter  
Untergaph

[15]

Weg

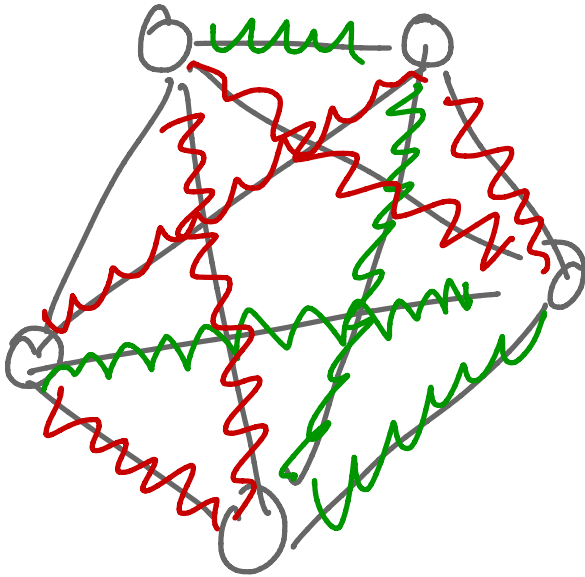


Kreis

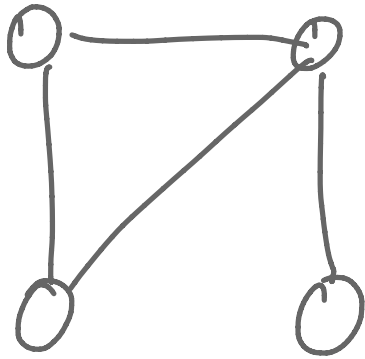


kein UG

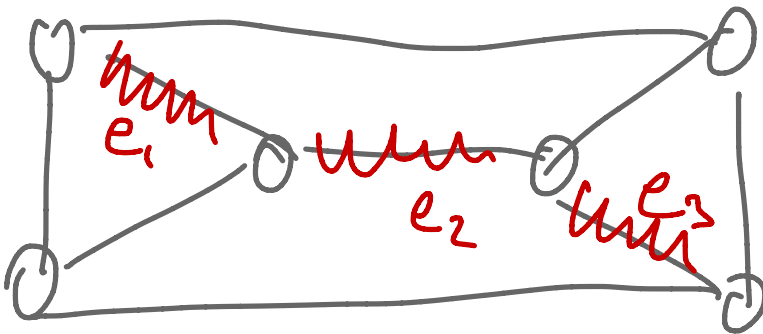
[16]



Hamilton-Wege in  $G$   
Hamilton-Kreis in  $G$



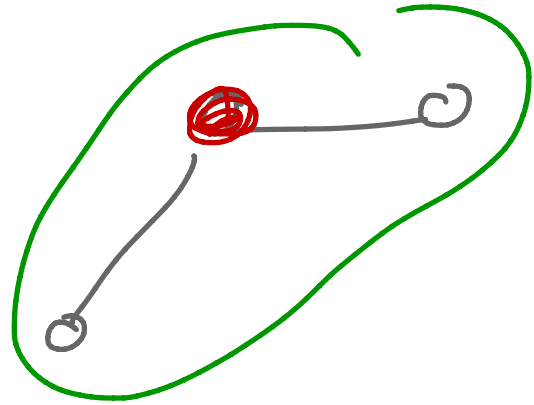
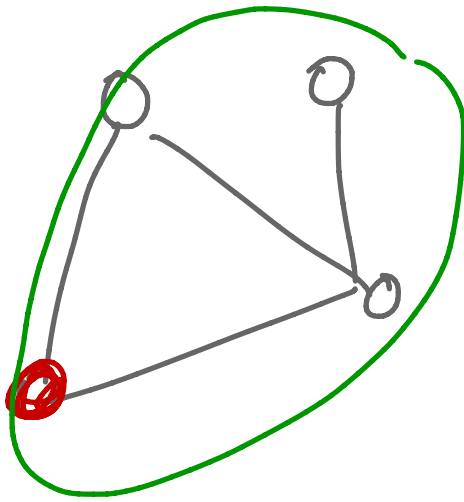
hat keine  
Hamilton-Kreis



H

$\{e_1, e_2, e_3\}$  ist ein Weg in H

[17]



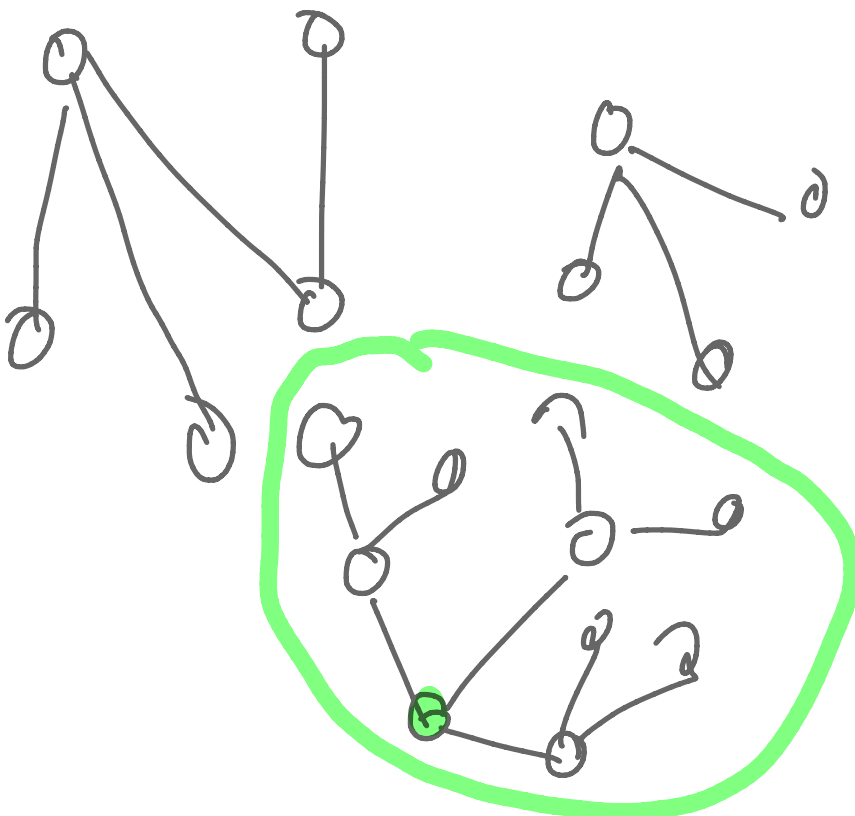
G

①

nicht zusammenhängend (keine  $\bullet - \bullet$ -Ueg)

3 Zusammenhangskomponenten

[18]



[19] Begründung: Sei  $\emptyset \neq W \subseteq E(G)$

inklusionsmaximal unter den Mengen in  $G$ ;

dann haben die beiden Endknoten

von  $W$  jeweils Grad 1.